

P5: Algebraic Expressions

1. The expression $(2\sqrt{x} + y)(2\sqrt{x} - y) + (2 - y)^2$ simplifies to

- A) $4x - 4y + 4$
- B) $4x^2 - 4y + 4$
- C) $4x - 4y - 4$
- D) $2y^2 + 4x - 4y + 4$
- E) $4x + 4y + 4$

2. The sum of all the coefficients of the polynomial $(x^2 - 2)^3 - (x^6 + 8)$ is

- A) -10
- B) -6
- C) 22
- D) 6
- E) 2

3. If $x^2 + \frac{1}{x^2} = 3$, then $\left(x - \frac{1}{x}\right)^2 =$

A) 1

B) -1

C) -4

D) 4

E) 9

4. The coefficient of xy^2 in the expansion of the expression $x(2x - y)(y + 2x) - (x + y^2)^2$ is:

A) -3

B) 1

C) -2

D) -4

E) 2

5. $\left(1 + \frac{x}{y}\right)^2 - \left(1 - \frac{x}{y}\right)^2 = ?$

A) $\frac{4x}{y}$

B) $\frac{2x}{y}$

C) $-\frac{4x}{y}$

D) $\frac{x}{y}$

E) $-\frac{x}{y}$

6. When simplified, the expression $8x^3 - 6x^2 - 1 - (2x - 1)^3$, is

A) a binomial of degree 2

B) a binomial of degree 1

C) a trinomial of degree 2

D) a monomial of degree 2

E) a monomial of degree

7. If the coefficient of xy in the product $(Mx + y)^2 \left(x - 1 - \frac{x}{y} \right)$ is -7,

then $M =$

A) 3

B) 9

C) $-\frac{7}{2}$

D) $\frac{7}{2}$

E) -3

8. Which one of the following is NOT a polynomial?

A) $x^3 - 4x^2 + 2\sqrt{x}$

B) $x^3 - 3x^2 + \sqrt{5}x$

C) $\sqrt{3}x^4 - \sqrt{5}x^2 - 1$

D) $x^2 - 4^{-1}x + \sqrt{12}$

E) $-\frac{1}{3}$

9. The expression $(a^2 + b^2)^2 - (a^2 - b^2)^2$ simplifies to

A) $4a^2b^2$

B) $2a^2b^2$

C) $2a^2$

D) $4a^4b^4$

E) $2a^4b^4$

10. The expression $(x + 2 + \sqrt{x^2 + 2})(x + 2 - \sqrt{x^2 + 2})$, is

A) a binomial of degree 1.

B) a trinomial of degree 2.

C) a binomial of degree 2.

D) a trinomial of degree 4.

E) a binomial of degree 4.

11. The coefficient of x^2y in the expression $(x^2 - 2y)^2 - (x - y)^3$, is

- A) -1
- B) 2
- C) -2
- D) 1
- E) -3

12. Which one of the following is a polynomial?

- A) $5x^4 + x + \sqrt{2}$
- B) $\frac{x+3}{3x^2+x+1}$
- C) $x^2 + 3x + 2x^{-2}$
- D) $\sqrt{x^2 + x + 4}$
- E) $2x^2 - x + \sqrt{x}$

13. The degree of the polynomial $(xy^2 - 1)^3(2x + 1)^2$ is

A) 11

B) 10

C) 9

D) 6

E) 5

14. If A is the leading coefficient and B is the coefficient of x in the

polynomial $P(x) = (2x - 3)^3 - (3x - 2)^2$ then $A + B =$

A) 74

B) 82

C) 64

D) 38

E) 56

15. If the coefficient of x^3 in the product $(x^4 + x^3 - kx^2 + x - 5)(3x^2 - 4x + k)$ is 18, then k is equal to:

- A) 3
- B) -2
- C) -5
- D) 2
- E) 1

16. The sum of the coefficients of x^2y and xy^2 in the expression $(2x - 3y)^3$ is

- A) 18
- B) -80
- C) -18
- D) -36
- E) 80

17. If $x + \frac{1}{x} = 3$, then by using the expansion of $\left(x + \frac{1}{x}\right)^3$, the value of $x^3 + \frac{1}{x^3}$ is equal to

A) 18

B) 27

C) 36

D) 0

E) 3

18. If the coefficient of x^3 in the product $(x^4 + x^3 - kx^2 + x - 5)(3x^2 - 4x + k)$ is 18, then k is equal to:

A) 3

B) -2

C) -5

D) 2

E) 1

19. When simplified, the expression $3y^2 \left(3x - \frac{2}{3}\right) \left(x + \frac{2}{9}\right)$ is a

- A) binomial of degree 4
- B) trinomial of degree 6
- C) trinomial of degree 4
- D) binomial of degree 2
- E) monomial of degree 2

20. The coefficient of x^3 in the product $2x(3x - 2)^3$ is equal to

- A) -108
- B) -54
- C) 54
- D) 72
- E) 27

21. The coefficient of x^2 in the product of $(2x^2 - 3x + 2)(-x^2 + 4x - 3)$ is

A) -20

B) -8

C) -16

D) 8

E) 22

22. If $(2x + 3)(2x - 3) - (3x - 2)^2 = ax^2 + bx + c$, then $a + b + c =$

A) -10

B) -6

23. The coefficient of x^4 in the expression $(2 - x^2)^3 - (2 + x^2)(2 - x^2)$,
is

A) 7

24. The coefficient of x in the expression $x(2x - 1)(2x + 1) - (x - 2)^3$ is

A) -11

B) -13

25. If $(A + 1)(A^2 + 1) = 3$, then $A^4 - 1 =$

- A) 3
- B) -3
- C) $3A - 1$
- D) $A - 3$
- E) $3A - 3$

26. When simplified, the expression $(3x - 1)^3 - 27x\left(x^2 - x + \frac{1}{3}\right)$ is

- A) a monomial of degree 0
- B) a binomial of degree 1
- C) a binomial of degree 2
- D) a trinomial of degree 3
- E) a monomial of degree 1

27. If the coefficient of xy in the product $(x - y)(x + y) - (Mx + y)^2$ is 8, then $M =$

A) 4

B) -4

C) -2

D) 8

E) -8

28. Which one of the following is NOT a polynomial of degree 2?

A) $x^2 + 2|x| + 1$

B) $(x - 2)(x + 2)$

C) $(x - 1)^2 + x^2$

D) $\pi x^2 + ex$

E) $x^2 - 4^{-1}x + \sqrt{5}$