

## 7.1: (Trigonometric identities)

$\frac{\cos x - \cot x}{1 - \sin x}$ is identical to	
A) $\tan x$ B) $\cot x$ C) $-\tan x$ D) 0 <b>E) <math>-\cot x</math></b>	Trigonometric Identities.
$\frac{\cos \theta}{1 + \sin \theta} + \frac{1 + \sin \theta}{\cos \theta} =$	
A) $2\sec \theta$ B) $2\csc \theta$ C) $2\cos \theta$ D) $2\sin \theta$ E) $2\cot \theta$	Trigonometric Identities.
Which one of the following statements is TRUE?	
A) $\tan^2 x = \sin^2 x \tan^2 x + \sin^2 x$ B) $\tan^2 x = 1 + \sec^2 x$ C) $\tan^2 x = (\sec x + 1)^2$ D) $\tan^2 x = 1 - \cot^2 x$ E) $\tan^2 x = \frac{\sin^2 x}{\sin^2 x - 1}$	Trigonometric Identities.

If  $A = \ln(\sec^2 x) - \ln(\tan^2 x)$ , then  $e^A - 1 =$

- A)  $\cot^2 x$
- B)  $\sec^2 x$
- C)  $\cos^2 x$
- D) 0
- E) 1

Trigonometric  
Identities.

The expression  $\frac{\cos x}{1-\sin x} - \tan x$  simplifies to

- A)  $\sec x$
- B)  $-\sec x$
- C)  $\csc x$
- D)  $-\csc x$
- E)  $2\tan x$

Trigonometric  
Identities.

$\ln(e^{\sin^2 x} e^{\cos^2 x}) =$

- A) 1
- B) 0
- C)  $e^{\sec x}$
- D)  $e^{\csc x}$
- E)  $2\cos x + 2\sin x$

Trigonometric  
Identities.

If  $A = 3\sin^2 \alpha + 3\cos^2 \alpha$  and  $B = 4\cot^2 \alpha - 4\csc^2 \alpha$ , then  $A + B =$

- A) -1
- B) 0
- C) 7
- D) 1
- E) -7

Trigonometric  
Identities.

The expression  $\frac{\tan^2 x}{1+\sec x}$  is identical to

- A)  $\frac{1-\cos x}{\cos x}$
- B)  $\frac{1-\cos x}{\sin x}$
- C)  $\frac{1-\sin x}{\sin x}$
- D)  $\frac{1+\cos x}{\cos x}$
- E)  $\frac{1+\sin x}{\sin x}$

Trigonometric  
Identities.

If  $\frac{(\tan x + \cot x)^2}{\sin^2 x - \sin^4 x} = \sec^m x \csc^n x$ , then  $m + n =$

- A) 8
- B) 6
- C) 4
- D) 10
- E) 12

Trigonometric  
Identities.

$\frac{\cot \theta - \tan \theta}{\sin \theta \cos \theta}$  is identical to:

A)  $\csc^2 \theta - \sec^2 \theta$

B)  $\sec^2 \theta - \csc^2 \theta$

C)  $1 - \sec^2 \theta$

D)  $\sec \theta + \csc \theta$

E)  $1 - \csc^2 \theta$

Trigonometric  
Identities.

If  $\pi < \theta < \frac{3\pi}{2}$ , then  $\cos \theta =$

A)  $-\frac{\cot \theta \sqrt{1+\cot^2 \theta}}{1+\cot^2 \theta}$

B)  $\frac{\cot \theta \sqrt{1+\cot^2 \theta}}{1+\cot^2 \theta}$

C)  $-\sqrt{1 + \cot^2 \theta}$

D)  $\frac{\sqrt{1+\cot^2 \theta}}{1+\cot^2 \theta}$

E)  $-\frac{\sqrt{1+\cot^2 \theta}}{1+\cot^2 \theta}$

Trigonometric  
Identities.

$$\frac{1 + \cot^2 \theta}{1 - \csc^2 \theta} =$$

A)  $-\sec^2 \theta$

B)  $\sec^2 \theta - 2$

C)  $-\csc^2 \theta$

D)  $\csc^2 \theta - 2$

E)  $-\csc^2 \theta - \sec^2 \theta$

Trigonometric  
Identities.

The expression  $\frac{1}{1+\csc x} - \frac{1}{1+\csc(-x)}$  simplifies to

A)  $2\sin x \sec^2 x$

B) 0

C)  $-2\sin x \sec^2 x$

D)  $-2\tan^2 x$

E) 2

Trigonometric  
Identities.

If  $\frac{\sec x + \csc x}{\tan x + \cot x} = a \sin x + b \cos x$ , then  $a + b =$

A) 2

B) 1

C) 3

D) 4

E) 0

Trigonometric  
Identities.

$$\tan \theta + \frac{1}{\sec \theta + \tan \theta} =$$

A)  $\sec \theta$

B)  $\cos \theta$

C)  $1 + \sin \theta$

D) 1

E)  $\sin \theta$

Trigonometric  
Identities.

$$(\sin^2 x)(1 + \cot x) + (\cos^2 x)(1 - \tan x) + \cot^2 x =$$

A)  $\csc^2 x$

B)  $\sec^2 x$

C)  $\tan^2 x$

D)  $\cot^2 x$

E)  $\cos^2 x$

Trigonometric  
Identities.

$$\tan^2(-x) - \sin^2(-x) - \cos^2(x) =$$

A)  $-1 + \tan^2 x$

B)  $\sec^2 x$

C)  $1 + \cot^2 x$

D)  $\csc^2 x$

E)  $\sin^2 x - \cos^2 x$

Trigonometric  
Identities.

$$(\cot x - \csc x)^2 =$$

A)  $\frac{1-\cos x}{1+\cos x}$

B)  $\frac{1+\cos x}{1-\cos x}$

C)  $\frac{\cos x - \sin x}{1+\cos x}$

D)  $\frac{\sin x}{1-\cos x}$

E)  $\frac{\cos x}{1+\cos x}$

Trigonometric  
Identities.

$\frac{\tan x - \cot x}{\tan x + \cot x}$  is identical to

- A)  $1 - 2\cos^2 x$
- B)  $1 - \tan^2 x$
- C)  $1 + \sec^2 x$
- D)  $1 + 2\sin^2 x$
- E)  $1 + 2\cos^2 x$

Trigonometric  
Identities.

Which one of the following statements is TRUE?

- A)  $\sin x = \sqrt{1 - \cos^2 x}$ , if  $0 \leq x \leq \pi$ .
- B)  $\csc x = \sqrt{1 + \cot^2 x}$
- C)  $\sqrt{\cos^2 x} = \cos x$  is an identity.
- D)  $\sin^3 x = \sin x(1 + \cos^2 x)$
- E)  $\cos^4 x + 1 = (\cos^2 x - 1)(\cos^2 x + 1)$

Trigonometric  
Identities.

$$\sin^3 \theta + \cos^3 \theta + \sin \theta \cos^2 \theta + \sin^2 \theta \cos \theta =$$

- A)  $\sin \theta + \cos \theta$
- B)  $\sin \theta - \cos \theta$
- C)  $\cos \theta - \sin \theta$
- D)  $2(\sin \theta + \cos \theta)$
- E)  $2\sin \theta \cos \theta$

Trigonometric  
Identities.

$$\sec^2 x - 2\sec x \tan x + \tan^2 x =$$

- A)  $\frac{1-\sin x}{1+\sin x}$
- B)  $\frac{1+\sin x}{1-\sin x}$
- C)  $\frac{1+\tan x}{1-\tan x}$
- D)  $\frac{1-\cos x}{1+\cos x}$
- E)  $\frac{1+\cos x}{1-\cos x}$

Trigonometric  
Identities.

If  $\csc \theta = \frac{x+1}{x}$ ,  $x > 0$ , then  $\cot \theta =$

- A)  $\frac{\sqrt{1+2x}}{x}$
- B)  $\frac{\sqrt{2x-1}}{x}$
- C)  $\frac{\sqrt{x^2+2x}}{x}$
- D)  $\frac{\sqrt{2x^2+2x+1}}{x}$
- E)  $\frac{1}{x}$

Trigonometric  
Identities.

If  $(\tan x \sin x)^2 = A \tan^2 x + B \sin^2 x$  is an identity, then  $A + B =$

- A) 0
- B) -2
- C) 2
- D) 1
- E) -1

Trigonometric  
Identities.

$2 \csc^2 x - 2 \csc x \cot x - 1 =$

- A)  $\frac{1-\cos x}{1+\cos x}$
- B)  $\frac{1+\cos x}{1-\cos x}$
- C)  $\frac{1-\sin x}{1+\cos x}$
- D)  $\frac{1+\sin x}{1-\cos x}$
- E)  $\frac{\cos x-1}{\sin x+1}$

Trigonometric  
Identities.

$$(\sin \theta + \csc \theta)^2 + (\cos \theta + \sec \theta)^2 - \tan^2 \theta - \cot^2 \theta =$$

A) 7

B) 3

C) 5

D) 0

E) 1

Trigonometric  
Identities.

$$\frac{2\tan x \cos^2 x - \tan x}{1 - \tan^2 x} =$$

A)  $\sin x \cos x$

B)  $\cos^2 x$

C)  $-\cot x \sin^2 x$

D)  $\cot x \sin^2 x$

E)  $-\sec x \csc^2 x$

Trigonometric  
Identities.

$$\tan^2 \frac{25\pi}{3} - \sec^2 60^\circ + 1 =$$

A) 0

B)  $\frac{3}{2}$

C)  $\frac{7}{4}$

D)  $\frac{3}{4}$

E) 2

Trigonometric  
Identities.

$$(\csc^2 x)(1 + \cos x)^2 =$$

A)  $\frac{\sec x \csc x + 1}{\sec x \csc x - 1}$

B)  $\frac{\sec x + \csc x}{\sec x - \csc x}$

C)  $\frac{\sec x + 1}{\sec x - 1}$

D)  $\frac{1}{\sec x - 1}$

E)  $\frac{\sec x + 1}{\sec x}$

Trigonometric  
Identities.

$$\frac{\cot^2 \theta}{1 + \csc \theta} =$$

A)  $\cos \theta - \sin \theta$

B)  $\frac{1 + \cos \theta}{\sin \theta}$

C)  $\frac{1 + \sin \theta}{\sin \theta}$

D)  $\frac{1 - \sin \theta}{\sin \theta}$

E)  $\frac{1 - \cos \theta}{\cos \theta}$

Trigonometric  
Identities.

$$\frac{\sin x (\tan x + 1) - 2 \tan x \cos x}{\sin x - \cos x} =$$

A)  $-\tan x$

B)  $\tan x$

C)  $\sec x$

D)  $-\sec x$

E)  $\sin x$

Trigonometric  
Identities.

$$\frac{1}{1 + \cos x} - \frac{1}{1 - \cos x} =$$

- A)  $-2\cot x \csc x$   
B)  $2\tan x \csc x$   
C)  $2\tan x \sec x$   
D)  $-2\cot x \sec x$   
E) -2

Trigonometric  
Identities.

$$\frac{\cot x + \csc x}{\sin x + \tan x}$$
 simplifies to:

- A)  $\csc x \cot x$   
B)  $\sin x \tan x$   
C)  $\sin x \cos x$   
D)  $\sec^2 x \tan x$   
E)  $\sin x \sec^2 x$

Trigonometric  
Identities.

$$\frac{2\sec \theta \csc \theta - 2\tan \theta \csc \theta}{(\sec \theta - \tan \theta)^2 + 1} =$$

- A)  $\cot \theta$   
B)  $\tan \theta$   
C)  $2\sec \theta$   
D)  $2\csc \theta$   
E)  $2\sec \theta \tan \theta$

Trigonometric  
Identities.

$$\tan^2 x(1 + \cot^2 x) =$$

A)  $\frac{1}{1-\sin^2 x}$

B)  $\frac{1}{1-\cos^2 x}$

C)  $\csc^2 x$

D)  $-\sec^2 x$

E)  $-\csc^2 x$

Trigonometric  
Identities.

When simplified, the expression  $(2\sin x + \cos x)^2 + (2\cos x - \sin x)^2 - 5$  is equal

A) 0

B) -5

C) 1

D)  $8\sin x \cos x$

E)  $3\sin^2 x + 5\cos^2 x - 5$

Trigonometric  
Identities.

The expression  $\frac{\sin \theta}{1-\cot \theta} + \frac{\cos \theta}{1-\tan \theta}$  simplifies to:

A)  $\sin \theta + \cos \theta$

B)  $\sin \theta - \cos \theta$

C)  $\frac{1}{\sin \theta - \cos \theta}$

D)  $\cos \theta - \sin \theta$

E)  $\frac{1}{\cos \theta - \sin \theta}$

Trigonometric  
Identities.

$\frac{\cos x - \cot x}{1 - \sin x}$  is identical to

- A)  $\tan x$
- B)  $\cot x$
- C)  $-\tan x$
- D) 0
- E)  $-\cot x$

Trigonometric Identities.

The expression  $(\sin \theta - \cos \theta)(\csc \theta + \sec \theta)$  simplifies to

- A)  $\tan \theta - \cot \theta$
- B)  $\sec \theta - \tan \theta$
- C)  $\csc \theta \cot \theta$
- D) 1
- E) 0

Trigonometric Identities.

$$\frac{\sin^3 \theta}{1 - \cos \theta} - \frac{\cos^3 \theta}{1 - \sin \theta} =$$

- (a)  $\sin \theta - \cos \theta$
- (b)  $\sin \theta \cos \theta$
- (c)  $\sin \theta + \cos \theta$
- (d)  $2\sin \theta$
- (e)  $2\cos \theta$

Trigonometric Identities.

Which one of the following statements is FALSE?

- A)  $\sec\left(\frac{\pi}{2} + x\right) = \csc x$
- B)  $\tan\left(x - \frac{\pi}{2}\right) = -\cot x$
- C)  $\sin\left(\frac{\pi}{2} + x\right) = \cos x$
- D)  $\sin\left(\frac{\pi}{2} - x\right) = \cos x$
- E)  $\cos\left(\frac{\pi}{2} - x\right) = \sin(\pi - x)$

Co-function Identities.

$$\cos\left(\frac{\pi}{2} - \sin^{-1}\left(-\frac{\sqrt{3}}{2}\right)\right) =$$

A)  $-\frac{1}{2}$

B)  $\frac{1}{2}$

C)  $-\frac{\sqrt{3}}{2}$

D)  $\frac{\sqrt{3}}{2}$

E)  $-\frac{\sqrt{2}}{2}$

Co-function  
Identities.

If  $\sec(\theta + 10^\circ) = \csc(2\theta - 40^\circ)$ , then one value of  $\theta$  is:

A)  $40^\circ$

B)  $20^\circ$

C)  $30^\circ$

D)  $50^\circ$

E)  $\frac{140^\circ}{3}$

Co-function  
Identities.

A value of angle  $\theta$  that makes  $\csc(3\theta - 15^\circ) = \sec(2\theta + 25^\circ)$  true is

A)  $16^\circ$

B)  $15^\circ$

C)  $20^\circ$

D)  $26^\circ$

E)  $10^\circ$

Co-function  
Identities.