

6.5 & 5.4: (Inverse Trigonometric Functions and Their Graphs)

If $\sec^{-1} 2 + \cos^{-1} x = \frac{\pi}{2}$, then $x =$

- A) $\frac{1}{2}$
- B) $-\frac{1}{2}$
- C) 1
- D) $\frac{\sqrt{3}}{2}$
- E) $-\frac{\sqrt{3}}{2}$

Inverse
Trigonometric
Functions.

$$\cos^{-1} \left(\cos \left(\frac{8\pi}{7} \right) \right) =$$

- A) $\frac{4\pi}{7}$
- B) $\frac{5\pi}{11}$
- C) $\frac{8\pi}{7}$
- D) $\frac{6\pi}{7}$
- E) $\frac{3\pi}{7}$

Inverse
Trigonometric
Functions.

$$\cos^{-1}\left(\sin\left(\frac{2\pi}{7}\right)\right) =$$

A) $\frac{3\pi}{14}$

B) $\frac{\pi}{14}$

C) $\frac{5\pi}{14}$

D) $\frac{2\pi}{7}$

E) $\frac{3\pi}{7}$

Inverse
Trigonometric
Functions.

If $\sec \theta = -\frac{2\sqrt{3}}{3}$ and $\cot \theta = \sqrt{3}$, then a value of θ is

A) 210°

B) 240°

C) 225°

D) 150°

E) 330°

Inverse
Trigonometric
Functions.

If $\csc \theta = -\frac{2\sqrt{3}}{3}$ and $\cot \theta = \frac{\sqrt{3}}{3}$, then a value of θ is

A) 240°

B) 210°

C) 225°

D) 330°

E) 150°

Inverse
Trigonometric
Functions.

Which one of the following statements is TRUE?

A) $\tan(\tan^{-1}(-11)) = -11$

B) $\tan^{-1}\left(\tan\frac{4\pi}{3}\right) = \frac{4\pi}{3}$

C) $\tan^{-1} x$ is an even function

D) $\tan^{-1} x = \frac{\sin^{-1} x}{\cos^{-1} x}$

E) $\tan^{-1}(-1) = \frac{\pi}{4}$

Inverse
Trigonometric
Functions.

$$\csc\left[\frac{\pi}{2} + \sin^{-1}\left(-\frac{3}{5}\right)\right] =$$

A) $\frac{5}{4}$

B) $-\frac{3}{5}$

C) $\frac{3}{5}$

D) $-\frac{5}{4}$

E) $\frac{5}{3}$

Inverse
Trigonometric
Functions.

Which one of the following statements is TRUE?

(a) $\sin^{-1}\left(\frac{\pi}{5}\right)$ is defined

(b) $\tan(\tan^{-1} 100)$ is undefined

(c) $\cos\left(\cos^{-1}\left(-\frac{1}{2}\right)\right) = \frac{1}{2}$

(d) $\tan^{-1} x = \frac{\sin^{-1} x}{\cos^{-1} x}$

(e) The functions $y = \cos^{-1} x$ and $y = \sin^{-1} x$ have the same range

Inverse
Trigonometric
Functions.

The exact value of $\sin^{-1} \left(\sin \frac{7\pi}{6} \right) + \tan \left(\cos^{-1} -\frac{1}{2} \right)$ is

(a) $-\frac{\pi}{6} - \sqrt{3}$

(b) $\frac{7\pi}{6} + \frac{\sqrt{3}}{3}$

(c) $\frac{\pi}{6} + \sqrt{3}$

(d) $\frac{5\pi}{6} - 1$

(e) $-\frac{\pi}{6} + \sqrt{3}$

Inverse
Trigonometric
Functions.

$$\sin^{-1} \left(\cos \left(\frac{5\pi}{11} \right) \right) =$$

A) $\frac{\pi}{22}$

B) $\frac{5\pi}{11}$

C) $\frac{20\pi}{11}$

D) $\frac{\pi}{11}$

E) $\frac{19\pi}{22}$

Inverse
Trigonometric
Functions.

If the domain of $f(x) = \pi + 5\cos^{-1} \left(\frac{x}{2} + b \right)$ is $[3,7]$, then $2b + 1 =$

A) -4

B) -5

C) 4

D) 5

E) 6

Inverse
Trigonometric
Functions.

The exact value of $\cos^{-1} \left(\cos \frac{10\pi}{3} \right)$, is

A) $\frac{2\pi}{3}$

B) $\frac{\pi}{3}$

C) $\frac{4\pi}{3}$

D) $\frac{10\pi}{3}$

E) undefined

Inverse
Trigonometric
Functions.

The range of $y = -\cos^{-1}(1 - 3x) - \pi$, is

A) $[-2\pi, -\pi]$

B) $[\pi - 1, \pi + 1]$

C) $\left[-\frac{3\pi}{2}, -\frac{\pi}{2} \right]$

D) $\left[0, \frac{2}{3} \right]$

E) $\left[-\frac{3\pi}{2}, \frac{\pi}{2} \right]$

Inverse
Trigonometric
Functions.

The exact value of $\cos^{-1} \left[\cos \left(\frac{5\pi}{4} \right) \right]$ is

A) $\frac{3\pi}{4}$

B) $\frac{\pi}{4}$

C) $\frac{5\pi}{4}$

D) $-\frac{\pi}{4}$

E) undefined

Inverse
Trigonometric
Functions.

$$\cos^{-1}\left(-\frac{1}{2}\right) - \tan^{-1}\left(\frac{\sqrt{3}}{3}\right) =$$

A) $\frac{\pi}{2}$

B) $\frac{3\pi}{2}$

C) $\frac{\pi}{3}$

D) $\frac{5\pi}{6}$

E) $\frac{7\pi}{4}$

Inverse
Trigonometric
Functions.

$$\tan\left[\sin^{-1}\left(-\frac{5}{13}\right)\right] =$$

A) $-\frac{5}{12}$

B) $-\frac{4}{5}$

C) $\frac{12}{5}$

D) $-\frac{12}{5}$

E) $\frac{5}{12}$

Inverse
Trigonometric
Functions.

The exact value of $\cos\left(\sin^{-1}\left(-\frac{3}{5}\right)\right)$ is equal to

(a) $\frac{4}{5}$

(b) $-\frac{4}{5}$

(c) $\frac{3}{4}$

(d) $-\frac{3}{4}$

(e) $\frac{3}{5}$

Inverse
Trigonometric
Functions.

From the adjacent figure $\theta =$

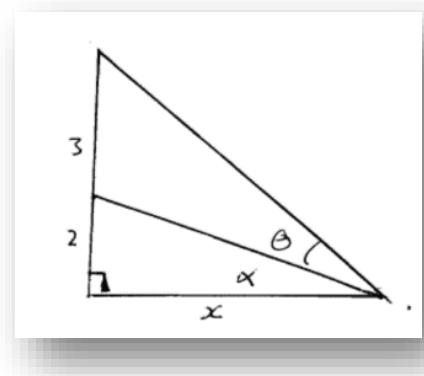
A) $\tan^{-1}\left(\frac{5}{x}\right) - \tan^{-1}\left(\frac{2}{x}\right)$

B) $\frac{1}{5}\tan^{-1}\left(\frac{5}{x}\right)$

C) $\tan^{-1}\left(\frac{x}{5}\right)$

D) $\tan^{-1}\left(\frac{2}{x}\right)$

E) $\tan^{-1}\left(\frac{3}{x}\right) - \tan^{-1}\left(\frac{5}{x}\right)$



Inverse
Trigonometric
Functions.

$$\tan^{-1}\left(\tan\frac{3\pi}{4}\right) =$$

A) $-\frac{\pi}{4}$

B) $\frac{\pi}{4}$

C) $-\frac{3\pi}{4}$

D) $\frac{3\pi}{4}$

E) undefined

Inverse
Trigonometric
Functions.

Which one of the following statements is TRUE?

A) $\tan^{-1}\left(\tan\frac{4\pi}{3}\right) = \tan^{-1}\left(\tan\frac{\pi}{3}\right)$

B) $\sin^{-1}\left(\sin\frac{5\pi}{6}\right) = \frac{5\pi}{6}$

C) $\tan^{-1} x = \left(\frac{\sin x}{\cos x}\right)^{-1}$

D) $\cos^{-1}(\cos x) = x$ for $-1 \leq x \leq 1$

E) $y = \sin^{-1} x$ is an even function.

Inverse
Trigonometric
Functions.

If $\arcsin\left(y - \frac{\pi}{3}\right) = \frac{\pi}{6}$, then y is equal to:

- A) $\frac{3+2\pi}{6}$
- B) $\frac{3-2\pi}{6}$
- C) $\frac{5\pi}{6}$
- D) $-\frac{3\sqrt{3}+2\pi}{6}$
- E) $-\frac{3\sqrt{3}}{6}$

Inverse
Trigonometric
Functions.

$$\sin^{-1}\left[\sin\frac{3\pi}{5}\right] - \cos^{-1}\left[\cos\frac{3\pi}{5}\right] =$$

- A) $\frac{6\pi}{5}$
- B) $-\frac{6\pi}{5}$
- C) $\frac{\pi}{5}$
- D) π
- E) $-\frac{\pi}{5}$

Inverse
Trigonometric
Functions.

$$\tan^{-1}\left(\tan\frac{3\pi}{4}\right) + \sin\left(\sin^{-1}\frac{\pi}{4}\right) =$$

- A) 0
- B) $-\frac{\pi}{2}$
- C) $\frac{\pi}{2}$
- D) $-\frac{\pi}{4} + \frac{\sqrt{2}}{2}$
- E) π

Inverse
Trigonometric
Functions.

The domain D and the range R of the function $f(x) = \pi + \cos^{-1}(x - 1)$ are

- A) $D = [0,2]$ and $R = [\pi, 2\pi]$
- B) $D = [0,2]$ and $R = [0,2\pi]$
- C) $D = [-1,1]$ and $R = [\pi, 2\pi]$
- D) $D = [-1,1]$ and $R = [0,2\pi]$
- E) $D = [0,2]$ and $R = [-\pi, \pi]$

Inverse
Trigonometric
Functions.

If the domain of the function $f(x) = \frac{\pi}{2} - 3\sin^{-1}(2x - 3)$ is $[m, n]$. then $m + n =$

- A) 3
- B) 4
- C) 2
- D) $-\pi$
- E) π

Inverse
Trigonometric
Functions.

$$\sin^{-1}\left(\frac{3}{5}\right) + \cos^{-1}\left(-\frac{4}{5}\right) =$$

A) $\frac{7}{5}$

B) $\frac{\pi}{2}$

C) π

D) $\frac{-1}{5}$

E) $\frac{3\pi}{2}$

Inverse
Trigonometric
Functions.

$$\cos^{-1}\left(\sin\frac{\pi}{5}\right) =$$

A) $\frac{3\pi}{10}$

B) $\frac{3\pi}{20}$

C) $\frac{3\pi}{5}$

D) $\frac{\pi}{10}$

E) $\frac{2\pi}{5}$

Inverse
Trigonometric
Functions.

$$\text{The value of } \cos^{-1}\frac{1}{2} + \sin^{-1}\left(\sin\frac{7\pi}{6}\right)$$

A) $\frac{\pi}{6}$

B) $\frac{\pi}{2}$

C) $\frac{3\pi}{2}$

D) $\frac{4\pi}{3}$

E) π

Inverse
Trigonometric
Functions.

The range of the function $y = \frac{\pi}{2} + 2\cos^{-1}(x + 1)$ is:

- A) $\left[\frac{\pi}{2}, \frac{5\pi}{2}\right]$
- B) $[0, \pi]$
- C) $[0, 2]$
- D) $\left[\frac{\pi}{2} - 1, \frac{\pi}{2} + 1\right]$
- E) $\left[-\frac{\pi}{2}, \frac{3\pi}{2}\right]$

Inverse
Trigonometric
Functions.

If $\arctan \frac{\sqrt{3}}{3} = x$ and $\arccos \left(-\frac{1}{2}\right) = y$, then $x + y =$

- A) $\frac{5\pi}{6}$
- B) π
- C) $\frac{7\pi}{3}$
- D) $\frac{4\pi}{3}$
- E) $\frac{7\pi}{6}$

Inverse
Trigonometric
Functions.

The solution of the equation $\cos^{-1} x + \tan^{-1} \frac{5}{12} = \frac{\pi}{2}$ is

- A) $\frac{5}{13}$
- B) $-\frac{12}{13}$
- C) $\frac{13}{12}$
- D) $-\frac{13}{5}$
- E) $\frac{7}{12}$

Inverse
Trigonometric
Functions.

Which of the following statements is FALSE?

- A) the domain of $y = \cos^{-1}(x + 1)$ is $[0, 2]$
- B) $\tan(\tan^{-1} x) = x$, for any real number x .
- C) the range of $y = 2\sin^{-1} x$ is $[-\pi, \pi]$
- D) $\sin^{-1} x + \sin^{-1}(-x) = 0, -1 \leq x \leq 1$
- E) $\cos^{-1}\left(\cos\frac{x}{2}\right) = \frac{x}{2}$ if $0 \leq x \leq 2\pi$

Inverse
Trigonometric
Functions.

The solution set of the equation $2\cos^{-1}\left(\frac{x-\pi}{3}\right) = 2\pi$ is

- A) $\{\pi - 3\}$
- B) $\{\pi + 2\}$
- C) $\{4 - \pi\}$
- D) $\{2\pi - 3\}$
- E) $\{\pi\}$

Inverse
Trigonometric
Functions.

The graph of the function $y = \frac{1}{3}\tan^{-1} 2x - \frac{\pi}{3}$ has

- A) range = $\left(-\frac{\pi}{2}, -\frac{\pi}{6}\right)$, domain = $(-\infty, \infty)$
- B) range = $\left(\frac{\pi}{6}, \frac{\pi}{2}\right)$, domain = $(-\infty, \infty)$
- C) range = $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$, domain = $(-\infty, \infty)$
- D) range = $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$, domain = $[-1, 1]$
- E) range = $(-\infty, \infty)$, domain = $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

Inverse
Trigonometric
Functions.

The domain of the function $y = \frac{\pi}{2} + 2\sin^{-1}\left(\frac{3}{2}x - \frac{5}{2}\right)$, is

- A) $\left[1, \frac{7}{3}\right]$
- B) $\left[\pi, \frac{7\pi}{3}\right]$
- C) $\left(-\infty, \frac{-\pi+5}{3}\right] \cup \left[\frac{\pi+5}{3}, \infty\right)$
- D) $\left[\frac{-\pi+5}{3}, \frac{\pi+5}{3}\right]$
- E) $(-\infty, 1] \cup \left[\frac{7}{3}, \infty\right)$

Inverse
Trigonometric
Functions.

The range of the function $y = \frac{\pi}{3} + \frac{1}{2}\sin^{-1}\left(x - \frac{\pi}{3}\right)$ is:

- A) $\left[\frac{\pi}{12}, \frac{7\pi}{12}\right]$
- B) $\left[\frac{\pi}{3} - \frac{1}{2}, \frac{\pi}{3} + \frac{1}{2}\right]$
- C) $\left(-\infty, \frac{\pi}{3} - \frac{1}{2}\right] \cup \left[\frac{\pi}{3} + \frac{1}{2}, \infty\right)$
- D) $\left[-\frac{\pi}{3}, \frac{\pi}{3}\right]$
- E) $\left(-\infty, \frac{\pi}{12}\right] \cup \left[\frac{7\pi}{12}, \infty\right)$

Inverse
Trigonometric
Functions.