

1) If  $(a, -\frac{3}{4})$  is a point on a **unit circle** on the terminal side of an angle  $\theta$ , in standard position, in quadrant III, then  $\cos \theta =$

A)  $-\frac{\sqrt{7}}{4}$

B)  $-\frac{\sqrt{7}}{2}$

C)  $-\frac{a}{4}$

D)  $-\frac{a}{2}$

E)  $-\frac{5}{4}$

2) The graph of  $y = -2 \sin\left(\frac{\pi x}{2}\right)$ , with  $0 < x < 4$ , is **increasing** on

A)  $[1, 3]$

B)  $[0, 1] \cup [3, 4]$

C)  $[\pi, 3\pi]$

D)  $[0, \pi] \cup [3\pi, 4\pi]$

E)  $[0, 4]$

3) The **range** of the function  $f(x) = 2 - \left| \cos \left( -\frac{\pi x}{4} \right) \right|$  is equal to

A)  $[1, 2]$

B)  $[0, 1]$

C)  $[2, 3]$

D)  $[-1, 0]$

E)  $[-2, 0]$

4) If  $P$  is the period, and  $S$  is the horizontal shift for the graph of the function

$$f(x) = \frac{1}{2} \sin \left( 2x + \frac{\pi}{4} \right), \quad \frac{\pi}{2} \leq x \leq \pi, \quad \text{then } P + S =$$

A)  $\frac{7\pi}{8}$

B)  $\frac{7\pi}{4}$

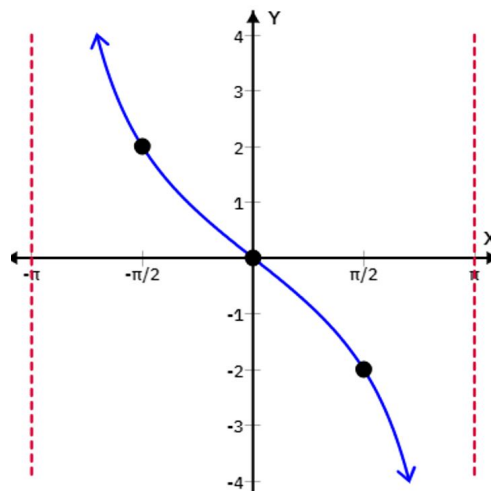
C)  $-\frac{3\pi}{8}$

D)  $-\frac{7\pi}{4}$

E)  $\frac{3\pi}{8}$

5) The given graph represents part of the graph of the function

- A)  $y = -2 \tan\left(\frac{1}{2}x\right)$
- B)  $y = -2 \tan\left(\frac{1}{2}x - \frac{\pi}{2}\right)$
- C)  $y = 2 \cot\left(\frac{1}{2}x\right)$
- D)  $y = 2 \cot\left(\frac{1}{2}x + \pi\right)$
- E)  $y = 2 \cot\left(\frac{1}{2}x - \pi\right)$



6) The graph of  $y = -\frac{1}{2} \cot(2x)$ ,  $-\frac{\pi}{4} < x \leq \frac{\pi}{2}$ , is **below** the  $x$ -axis on

- A)  $(0, \pi/4)$
- B)  $(\pi/4, \pi/2)$
- C)  $(-\pi/4, 0)$
- D)  $(-\pi/4, \pi/4)$
- E)  $(0, \pi/2)$

7) The **number** of the vertical asymptotes of the graph of  $y = \frac{2}{3} - \frac{3}{2} \csc(2x - \pi)$  in the interval  $(-\pi, \pi)$  is

A) 3

B) 2

C) 4

D) 5

E) 6

8) If  $[m, n]$  is the **domain** of  $f(x) = \frac{1}{2} \cos^{-1}\left(\frac{x}{2} - \frac{2}{3}\right)$ , then  $n - m =$

A) 4

B) 1

C) 2

D)  $-\frac{1}{2}$

E)  $\frac{1}{2}$

9) If  $\cos^{-1}x + \sin^{-1}\left(\frac{\sqrt{3}}{2}\right) = \frac{\pi}{2}$ , then  $x =$

A)  $\frac{\sqrt{3}}{2}$

B)  $\frac{1}{2}$

C)  $\frac{\sqrt{3}}{4}$

D)  $\frac{3}{4}$

E) 1

10)  $\sin^4 x - \cos^4 x =$

A)  $-\cos 2x$

B)  $-\sin 2x$

C)  $1 - 2\sin^2 x$

D)  $2\cos^2 x - 1$

E)  $\cos^2 x \sin^2 x$

11) If  $25 \cos^2 \theta - 16 = 0$ , where  $\frac{3\pi}{2} < \theta < 2\pi$ , then  $\cot \theta =$

A)  $-\frac{4}{3}$

B)  $\frac{4}{3}$

C)  $-\frac{3}{4}$

D)  $-\frac{\sqrt{3}}{2}$

E)  $\frac{\sqrt{3}}{2}$

12)  $\frac{\tan^2 x}{\sec^2 x} =$

A)  $1 - \cos^2 x$

B)  $\frac{1}{2} \sin^2 x$

C)  $1 - \sin^2 x$

D)  $1 + \cot^2 x$

E)  $\frac{1}{2} \csc^2 x$

13) The expression  $\cos\left(\frac{\pi}{2} - \alpha - \beta\right)$  simplifies to

A)  $\sin(\alpha + \beta)$

B)  $\sin(\alpha - \beta)$

C)  $\cos(\alpha + \beta)$

D)  $-\cos(\alpha - \beta)$

E)  $-\cos(\alpha + \beta)$

14)  $\tan\left(\frac{2\pi}{3} - \frac{\pi}{4}\right) =$

A)  $2 + \sqrt{3}$

B)  $2 - \sqrt{3}$

C)  $-2 + \sqrt{3}$

D)  $-2 - \sqrt{3}$

E)  $-1$

15) The expression  $\cot 67.5^\circ$ , is equal to

A)  $-1 + \sqrt{2}$

B)  $1 + \sqrt{2}$

C)  $2 + \sqrt{2}$

D)  $2 - \sqrt{2}$

E)  $-1 - \sqrt{2}$

16) If  $\csc \theta = -\frac{5}{3}$ ,  $\pi < \theta < \frac{3\pi}{2}$ , then  $\cos \frac{\theta}{2} =$

A)  $-\frac{\sqrt{10}}{10}$

B)  $\frac{\sqrt{10}}{10}$

C)  $-\frac{\sqrt{5}}{10}$

D)  $\sqrt{10}$

E)  $-\sqrt{10}$



17)  $\left(\sin \frac{x}{2} - \cos \frac{x}{2}\right)^2 =$

A)  $1 - \sin x$

B)  $1 + \cos x$

C)  $-\cos x$

D)  $-\sqrt{1 + \cos x}$

E)  $\sqrt{1 - \sin x}$

18) The **number** of all the **negative** solution(s) of the equation  $2\sin\left(x + \frac{2\pi}{3}\right) = \sqrt{3}$   
 $-\pi \leq x < 2\pi$ , is

A) 1

B) 0

C) 2

D) 3

E) 4

19) If  $0^\circ \leq x < 360^\circ$ , then the **number** of all the solution(s) of the equation

$$\tan^2 x + \tan x - \sqrt{3} \tan x = \sqrt{3}, \text{ is equal to}$$

- A) 4
- B) 1
- C) 5
- D) 6
- E) 2

20) The **solution set** of the equation  $3 \cos^2 x + 2 \cos x - 8 = 0$ ,  $0 \leq x < 2\pi$ , is

- A)  $\emptyset$
- B)  $\left\{ \frac{\pi}{3}, \frac{5\pi}{3} \right\}$
- C)  $\left\{ \frac{2\pi}{3}, \frac{4\pi}{3} \right\}$
- D)  $\left\{ \frac{\pi}{3}, \frac{2\pi}{3} \right\}$
- E)  $\left\{ \frac{2\pi}{3}, \frac{5\pi}{3} \right\}$