

1) Let  $i = \sqrt{-1}$ . If  $(3 - i) - (3 - i)^2 = x + iy$ , where  $x$  and  $y$  are real numbers, then  $3x + y =$

A) 0

B) 2

C) 10

D) - 2

E) - 10

2) Let  $f$  be a linear function such that  $f(-2) = \frac{1}{2}$  and  $f(1) = \frac{3}{2}$ , then

$$f\left(\frac{5}{2}\right) =$$

A)  $\frac{2}{3}$

B) - 2

C) 2

D) 0

E)  $-\frac{2}{3}$

3) Which ONE of the following statements is TRUE

- A) The slope of the line  $3x - 2 = 0$  is  $\frac{2}{3}$ .
- B) The line  $3x + 2y = 6$  is parallel to the line  $4y = -6x + 1$ .
- C) The line  $3x + 2y = 6$  is perpendicular to the line  $3y = -\frac{9}{2}x + 2$ .
- D) The slope of the line  $x = \frac{3}{7}y - 5$  is  $\frac{3}{7}$ .
- E) The slope of the line  $2y = 6$  is  $3$ .

4) The solution set, in interval notation, of the inequality  
 $-3|2x - 1| + 5 \geq -4$  is

- A)  $(-\infty, -1) \cup [2, \infty)$
- B)  $[-1, 4]$
- C)  $(-\infty, 2]$
- D)  $[-1, 2]$
- E)  $(-\infty, -1] \cup [4, \infty)$

5) The sum of all the solutions of the equation  $3x(x - 1) = 6$  is equal to

A)  $-1$

B)  $1$

C)  $-2$

D)  $-6$

E)  $2$

6) If  $f(x) = 3x$  and  $g(x) = x^3 - x$ , then which ONE of the following statements is TRUE ?

A)  $f \cdot g$  is an even function.

B)  $f - g$  is an even function.

C)  $\frac{f}{g}$  is an odd function.

D)  $\frac{g}{f}$  is an odd function.

E)  $f + g$  is an even function.

7) The sum of all the solutions of the equation  $8x^3 - 27 = 0$  is equal to

A)  $-\frac{3}{2}$

B) 3

C) -3

D)  $\frac{3}{2}$

E) 0

8) If the line through the points  $(1, 3)$  and  $(-3, b)$  is perpendicular to the line  $2x - 5y = 7$  then  $b =$

A)  $\frac{2}{5}$

B) -13

C) 13

D)  $\frac{18}{5}$

E) 2

9) The graph of the function  $f(x) = \begin{cases} 2x & \text{if } x \leq -1 \\ x^2 - 1 & \text{if } x > -1 \end{cases}$  is increasing

- A) on the interval  $(0, \infty)$
- B) on the interval  $(-\infty, \infty)$
- C) on the interval  $(-\infty, -1)$
- D) on the interval  $(-1, 0)$
- E) on the interval  $(-\infty, -1)$  and on the interval  $(0, \infty)$

10) Let  $\llbracket \cdot \rrbracket$  denotes the greatest integer function.

If  $f(x) = \begin{cases} x - 1 & \text{if } x \leq -2 \\ \llbracket 2x + 1 \rrbracket & \text{if } -2 < x \leq 4 \\ x^2 - 4x & \text{if } x > 4 \end{cases}$ , then  $(f \circ f)(\pi) =$

- A) 7
- B) 49
- C) 28
- D) 15
- E) 21

11) If the quadratic equation  $x^2 - kx + 3 = 0$  has exactly one solution then one value of  $k$  is

A) 3

B) 6

C) -3

D)  $3\sqrt{2}$

E)  $2\sqrt{3}$

12) Let  $i = \sqrt{-1}$ . If  $z = \frac{1 + 3i}{1 - i}$  is written in standard form, then  $z =$

A)  $2 + i$

B)  $2 - i$

C)  $-1 - 2i$

D)  $-1 + 2i$

E)  $1 + 2i$

- 13) If the graph of  $y = \frac{2 - x}{x + 3}$  is translated one unit down and two units to the left, then the equation of the new graph is

A)  $y = -\frac{2x + 5}{x + 5}$

B)  $y = \frac{x + 5}{x}$

C)  $y = \frac{-x}{x + 5}$

D)  $y = \frac{5}{x + 5}$

E)  $y = \frac{4 - x}{x + 1}$

- 14) The domain of the function  $f(x) = \frac{x - 2}{x^2 + 2x - 8}$  is

A)  $(-\infty, -4) \cup (2, \infty)$

B)  $(-\infty, -4) \cup (-4, \infty)$

C)  $(-4, 2) \cup (2, \infty)$

D)  $(-\infty, -4) \cup (-4, 2)$

E)  $(-\infty, -4) \cup (-4, 2) \cup (2, \infty)$

15) The solution set, in interval notation, of the inequality

$$-\frac{1}{3} \leq \frac{2-x}{5} < \frac{1}{2} \text{ is}$$

- A)  $[-3, 22]$
- B)  $(-\frac{1}{2}, \frac{2}{3}]$
- C)  $(-\frac{1}{2}, \frac{11}{3}]$
- D)  $(-22, 3]$
- E)  $(-\frac{9}{2}, \frac{11}{3}]$

16) If  $f(x) = 2x - 1$  and  $(f \circ g)(x) = 2x^2 - 4x + 1$ , then  $g(-1) =$

- A)  $-3$
- B)  $4$
- C)  $7$
- D)  $3$
- E)  $0$



17) If the point  $(1, -3)$  lies on the graph of the function  $y = f(x)$  then a point that lies on the graph of the function  $y = 2f\left(\frac{x}{2}\right) + 1$  is

A)  $\left(\frac{1}{2}, -\frac{1}{2}\right)$

B)  $(2, -5)$

C)  $\left(\frac{1}{2}, -5\right)$

D)  $\left(2, -\frac{1}{2}\right)$

E)  $(2, 7)$

18) The solution set, in interval notation, of the inequality  $\frac{2x - 3}{x + 1} \leq 1$  is

A)  $(-1, 4]$

B)  $(-\infty, -4]$

C)  $(-1, 2]$

D)  $(-\infty, -1) \cup [2, \infty)$

E)  $(-\infty, -1) \cup [4, \infty)$

19) The product of all the solutions of  $\sqrt{3x + 1} + 1 = x + 2$ , is equal to

- A) 1
- B) - 1
- C) 2
- D) 0
- E) - 2

20) The sum of all the solutions of  $\sqrt{(x - 1)^2} = |1 - x|^2 - 12$  is equal to

- A) - 2
- B) - 4
- C) 4
- D) 2
- E) 0

Answer Key

Testname: MAJOR 2 MATH001 222 CODE 001

- 1) E
- 2) C
- 3) B
- 4) D
- 5) B
- 6) A
- 7) E
- 8) C
- 9) E
- 10) E
- 11) E
- 12) D
- 13) A
- 14) E
- 15) C
- 16) B
- 17) B
- 18) A
- 19) D
- 20) D